

Introduction

Concept of percentage is similar to ratios and fractions.

In simple terms, percentage means 'out of one hundred'. We denote it as %

$$x\% = \frac{x}{100}$$

% means hundredths.

Examples:

Example 1- Express each of the following as a fraction:

(a) 36%

$$\text{Solution: } 36\% = \frac{36}{100} = \frac{18}{50} = \frac{9}{25}$$

(b) 120%

$$\text{Solution: } 120\% = \frac{120}{100} = \frac{6}{5} = 1\frac{1}{5}$$

(c) 0.8%

$$\text{Solution: } 0.8\% = \frac{0.8}{100} = \frac{8}{1000} = \frac{4}{500} = \frac{2}{250} = \frac{1}{125}$$

Example 2 – Express each of the following as a decimal:

(a) 80%

$$\text{Solution: } 80\% = \frac{80}{100} = \frac{4}{5} = 0.8$$

(b) 8%

$$\text{Solution: } 8\% = \frac{8}{100} = \frac{2}{25} = 0.08$$

(c) 205%

Solution: $205\% = \frac{205}{100} = 2.05$

Example 3 – Express each of the following fractions as a percentage:

(a) $\frac{7}{25}$

Solution: $\left(\frac{7}{25} \times 100\right)\% = 28\%$

(b) $\frac{5}{8}$

Solution: $\left(\frac{5}{8} \times 100\right)\% = \frac{500}{8}\% = \frac{125}{2}\% = 62\frac{1}{2}\%$

(c) $\frac{11}{6}$

Solution: $\left(\frac{11}{6} \times 100\right)\% = \left(\frac{1100}{6}\right)\% = \frac{550}{3}\% = 183\frac{1}{3}\%$

Example 4 – Convert the ratio 3: 4 to percentage.

Solution: Ratio = $\frac{3}{4}$

We have to convert this ratio into percentage

$\Rightarrow \left(\frac{3}{4} \times 100\right)\% = \frac{300}{4}\% = 75\%$

Example 5 – Express 36% as a ratio.

Solution: 36%

$$36\% = \frac{36}{100} = \frac{9}{25}$$

Thus, ratio = 9: 25

Example 6 – Which is largest in $16\frac{2}{3}\%$, $\frac{2}{15}$, and 0.12?

Solution: We are given with three numbers $16\frac{2}{3}\%$, $\frac{2}{15}$ and 0.12

We have to find the largest number among them.

$$\text{First number} = 16\frac{2}{3}\% = \frac{50}{3}\% = \frac{50}{3} \times \frac{1}{100} = \frac{1}{6} = 0.166 \dots$$

$$\text{Second number} = \frac{2}{15} = 0.133\dots$$

$$\text{Third number} = 0.12$$

Largest number is 0.166..

Thus, $16\frac{2}{3}\%$ is the largest among three numbers.

Example 7 – (a) What per cent of 120 is 90?

(b) What per cent of 1 kg is 5 g?

(c) What per cent of 3.5 L is 150mL?

$$\text{Solution: (a) Required percentage} = \left(\frac{90}{120} \times 100\right)\% = 75\%$$

(b) Since $1\text{kg} = 1000\text{g}$

$$\text{Required percentage} = \left(\frac{5}{1000} \times 100\right)\% = 0.5\%$$

(c) Since $1\text{l} = 1000\text{ml}$

$$\text{Required percentage} = \left(\frac{150}{3500} \times 100\right)\% = \frac{30}{7}\% = 4\frac{2}{7}\%$$

Example 8: Find $7\frac{1}{2}\%$ of Rs 2400

$$\text{Solution: } 7\frac{1}{2}\% \times \text{Rs}2400$$

$$\Rightarrow \frac{15}{2} \times \frac{1}{100} \times 2400 = \text{Rs}180$$

Example 9 – If 26% of a number is 65, find the number.

Solution: Let a number be x

Then, according to given question,

$$26\% \times x = 65$$

$$\Rightarrow \frac{26}{100} \times x = 65$$

$$\Rightarrow x = \frac{65 \times 100}{26} = 250$$

Example 10: Sarita spends 65% of her salary and the rest she saves. If she saves Rs 2940 per month, what is her monthly salary?

Solution: Let the monthly salary of sarita be $Rs\ x$

$$\text{Expenditure of sarita} = 65\% \times x = \frac{65}{100}x = Rs\ \frac{13x}{20}$$

$$\text{Savings of sarita} = Rs\ \left(x - \frac{13x}{20}\right) = Rs\ \frac{7x}{20}$$

$$\text{Savings} = Rs2940$$

$$\Rightarrow \frac{7x}{20} = 2940$$

$$\Rightarrow x = \frac{2940 \times 20}{7} = 420 \times 20 = 8400$$

Thus, monthly salary of sarita = $Rs8400$

Example 11: In a class, the girls are 60% of the total number of students and the boys are 18 in number. How many students are there in the class?

Solution: Let total number of students in the class be x

Percentage of girls = 60%

Thus, percentage of boys = 40%

Number of boys = 18

$$\Rightarrow 40\% \times x = 18$$

$$\Rightarrow \frac{40x}{100} = 18$$

$$\Rightarrow \frac{2x}{5} = 18$$

$$\Rightarrow x = \frac{18 \times 5}{2} = 45$$

Therefore, total number of students in the class is 45

Example 12: A number is increased by 20% and then decreased by 20%. Find the net increase or decrease per cent?

Solution: Let the number be x

When number is increased by 20%,

$$\text{New number} = 120\% \times x = \frac{120x}{100} = \frac{6x}{5}$$

Then, resulting number is decreased by 20%

$$\text{New number} = 80\% \times \frac{6x}{5} = \frac{80}{100} \times \frac{6x}{5} = \frac{24x}{25}$$

$$\text{Thus, net decrease} = x - \frac{24x}{25} = \frac{x}{25}$$

$$\text{Net decrease percentage} = \left(\frac{x}{25} \times \frac{1}{x} \times 100 \right) \% = 4\%$$

Example 13: In an examination, one requires 40% marks to pass. Rahul gets 185 marks and fails by 15 marks. What are the maximum marks?

Solution: Let the maximum marks be x

Marks obtained by Rahul = 185

But he fails by 15 marks

So, passing marks = $185 + 15 = 200$

And passing percentage = 40%

$$\Rightarrow 40\% \times x = 200$$

$$\Rightarrow \frac{40}{100} \times x = 200$$

$$\Rightarrow x = \frac{200 \times 100}{40} = 500$$

Therefore, maximum marks = 500

Example 14: Out of her total monthly salary, Tanvy spends 30% on house rent and 60% of the rest on household expenditure. If she saves Rs 10500, what is her total monthly salary?

Solution: Let the total monthly salary of tanvi be Rs x

$$\text{Money spent on house rent} = 30\% \times x = \frac{30x}{100} = \frac{3x}{10}$$

$$\text{Remaining money} = x - \frac{3x}{10} = \frac{7x}{10}$$

$$\text{Money spent on household expenses} = 60\% \times \frac{7x}{10} = \frac{60}{100} \times \frac{7x}{10} = \frac{21x}{50}$$

$$\text{Her savings} = \frac{7x}{10} - \frac{21x}{50}$$

$$= \frac{35x - 21x}{50} = \frac{14x}{50} = \frac{7x}{25}$$

Now, savings are given to be 10500

$$\Rightarrow \frac{7x}{25} = 10500$$

$$\Rightarrow x = \frac{10500 \times 25}{7} = 1500 \times 25 = 37500$$

Therefore, monthly income of tanvi = Rs 37500

Example 15: The price of sugar goes up by 20%. By how much per cent must a housewife reduce her consumption of sugar so that the expenditure on sugar remains the same?

Solution: Let us assume the consumption of sugar be 1 unit

And let the cost of 1 unit of sugar be Rs100

Now, if the price goes up by 20%

New cost of 1 unit = Rs 120

Since, Rs 120 = Cost of 1 unit

Then, Rs 1 = Cost of $\frac{1}{120}$ unit

Rs 100 = Cost of $\frac{1}{120} \times 100 = \frac{5}{6}$ units

Thus, cost of $\frac{5}{6}$ units of sugar = Rs 100

Reduction in consumption = $1 - \frac{5}{6} = \frac{1}{6}$

Percentage of reduction in consumption = $\left(\frac{1}{6} \times \frac{1}{1} \times 100\right)\% = \frac{50}{3}\% = 16\frac{2}{3}\%$

Example 16: The population of a town increases by 6% annually. If the present population is 17490, what was it a year ago?

Solution: Let the population of town a year ago be x

It is given that population of a town increase by 6% annually

Thus, present population = $106\% \times x = \frac{106x}{100} = \frac{53x}{50}$

Present population is given to be 17490

$$\Rightarrow \frac{53x}{50} = 17490$$

$$\Rightarrow x = \frac{17490 \times 50}{53} = 330 \times 50 = 16500$$

Therefore, population a year ago was 16500

Example 17: The value of a machine depreciates every year by 10%. If the present value of the machine be Rs 99000, what was its value last year?

Solution: Let value of machine last year be Rs x

It is given that value depreciates by 10% every year

$$\text{Thus, present value of machine} = 90\% \times x = \frac{90x}{100} = \frac{9x}{10}$$

Also, present value of machine is given to be Rs 99000

$$\Rightarrow \frac{9x}{10} = 99000$$

$$\Rightarrow x = \frac{99000 \times 10}{9} = 110000$$

Therefore, value of machine last year was Rs 110000

Example 18: A's income is 60% more than that of B. By what per cent is B's income less than A's?

Solution: Let the income of B be Rs 100

Given that income of A is 60% more than B

Thus, income of A = Rs 160

Now, if income of A is Rs 160, then income of B = Rs 100

If income of A is Rs 1, then income of B = $\frac{100}{160}$

If income of A is Rs 100, then income of B = $\frac{100 \times 100}{160} = \text{Rs } 62.5$

Thus, B's income is less than A's income by $(100 - 62.5) = 37.5\%$

Exercise 9A

Question 1: Express each of the following as a fraction:

(a) $48\% = \frac{48}{100} = \frac{12}{25}$

(b) $220\% = \frac{220}{100} = \frac{11}{5} = 1\frac{2}{5}$

(c) $2.5\% = \frac{2.5}{100} = \frac{25}{1000} = \frac{1}{40}$

Question 2: Express each of the following as a decimal:

(a) $6\% = \frac{6}{100} = 0.06$

(b) $72\% = \frac{72}{100} = 0.72$

(c) $125\% = \frac{125}{100} = 1.25$

Question 3: Express each of the following as a percentage:

(a) $\frac{9}{25}$

Solution: $(\frac{9}{25} \times 100)\% = 36\%$

(b) $\frac{3}{125}$

Solution: $(\frac{3}{125} \times 100)\% = \frac{300}{125}\% = \frac{12}{5}\% = 2.4\%$

(c) $\frac{12}{5}$

Solution: $(\frac{12}{5} \times 100)\% = 240\%$

Question 4: Convert the ratio 4:5 to percentage.

Solution: Ratio = 4: 5

We have to convert this ratio into percentage:

$$\left(\frac{4}{5} \times 100\right)\% = 80\%$$

Question 5: Express 125% as a ratio.

Solution: 125%

$$\frac{125}{100} = \frac{25}{20} = \frac{5}{4}$$

Thus, Ratio = 5: 4

Question 6: Which is largest in $6\frac{2}{3}\%$, $\frac{3}{20}$ and 0.14?

Solution: We are given with three numbers $6\frac{2}{3}\%$, $\frac{3}{20}$ and 0.14

We have to find the largest number among them.

$$\text{First number} = 6\frac{2}{3}\% = \frac{20}{3}\% = \frac{20}{3} \times \frac{1}{100} = \frac{1}{15} = 0.066 \dots$$

$$\text{Second number} = \frac{3}{20} = 0.15$$

Third number = 0.14

Largest number is 0.15

Thus $\frac{3}{20}$ is the largest among three numbers

Question 7: (a) What per cent of 150 is 96?

(b) What per cent of 5 kg is 200 g?

(c) What per cent of 2 litres is 250 mL?

Solution: (a) $\left(\frac{96}{150} \times 100\right)\% = \frac{960}{15}\% = 64\%$

(b) Since 1kg = 1000g

$$\left(\frac{200}{5000} \times 100\right)\% = 4\%$$

(c) Since 1l = 1000 ml

$$\left(\frac{250}{2000} \times 100\right)\% = 12.5\%$$

Question 8: Find $4\frac{1}{2}\%$ of Rs 3600

Solution: $4\frac{1}{2}\% \times 3600$

$$= \frac{9}{2}\% \times 3600 = \frac{9}{2} \times \frac{1}{100} \times 3600 = 162$$

Question 9: If 16% of a number is 72, find the number.

Solution: Let a number be x

According to given question,

$$16\% \times x = 72$$

$$\Rightarrow \frac{16x}{100} = 72$$

$$\Rightarrow x = \frac{72 \times 100}{16} = \frac{7200}{16} = 450$$

Question 10: A man saves 18% of his monthly income. If he saves Rs 3780 per month, what is his monthly income?

Solution: Let monthly income of man be Rs x

Given that $18\% \times x = 3780$

$$\Rightarrow \frac{18x}{100} = 3780$$

$$\Rightarrow x = \frac{3780 \times 100}{18} = 210 \times 100 = 21000$$

Thus, the monthly income of man = Rs 21000

Question 11: A football team wins 7 games, which is 35% of the total games played. How many games were played in all?

Solution: Let total games played be x

Winning games = 7

According to given question,

$$\Rightarrow 35\% \times x = 7$$

$$\Rightarrow \frac{35x}{100} = 7$$

$$\Rightarrow x = \frac{700}{35} = 20$$

Thus, total football games played were 20

Question 12: Amit was given an increment of 20% on his salary. If his new salary is Rs 30600, what was his salary before the increment?

Solution: Let the salary of amit before the increment be Rs x

Increment = 20%

$$\Rightarrow \text{New salary} = 120\% \times x$$

Also, new salary is given to be Rs 30600

$$\Rightarrow 120\% \times x = 30600$$

$$\Rightarrow \frac{120x}{100} = 30600$$

$$\Rightarrow x = \frac{30600 \times 100}{120} = 5100 \times 5 = 25500$$

Thus, the salary before increment was Rs 25500

Question 13: Sonal attended her school on 204 days in a full year. If her attendance is 85%, find the number of days on which the school was opened.

Solution: Let the number of days on which school was opened be x days

Number of days sonal attended school = 204 days

Here, attendance = $85\% \times x$

$$\Rightarrow 85\% \times x = 204$$

$$\Rightarrow \frac{85x}{100} = 204$$

$$\Rightarrow x = \frac{204 \times 100}{85} = 12 \times 20 = 240$$

Thus, number of days school was opened = 240 days

Question 14: A's income is 20% less than that of B. By what per cent is B's income more than A's?

Solution: Let the income of B be Rs 100

Given that income of A is 20% less than B

Thus, income of A = Rs80

Now, if income of A is Rs80, then income of B = Rs100

If income of A is Rs1, then income of B = $\frac{100}{80}$

If income of A is Rs100, then income of B = $\frac{100 \times 100}{80} = Rs125$

Thus, B's income is more than A's income by $(125 - 100) = 25\%$

Question 15: The price of petrol goes up by 10%. By how much per cent must a motorist reduce the consumption of petrol so that the expenditure on it remains unchanged?

Solution: Let's assume the consumption of petrol be 1 unit

And let the cost of 1 unit of petrol be Rs100

Now, if the price goes up by 10%

New cost of 1 unit = Rs 110

Since Rs 110 = Cost of 1 unit

Then, Rs 1 = Cost of $\frac{1}{110}$ unit

Rs 100 = Cost of $\frac{1}{110} \times 100 = \frac{10}{11}$ units

Thus, cost of $\frac{10}{11}$ units of petrol = Rs 100

Reduction in consumption = $1 - \frac{10}{11} = \frac{1}{11}$

Percentage of reduction in consumption = $\left(\frac{1}{11} \times \frac{1}{1} \times 100\right)\% = \frac{100}{11}\% = 9\frac{1}{11}\%$

Question 16: The population of a town increases by 8% annually. If the present population is 54000, what was it a year ago?

Solution: Let the population of town a year ago be x

It is given that population of a town increase by 8% annually

Thus, present population = $108\% \times x = \frac{108x}{100} = \frac{54x}{50} = \frac{27x}{25}$

Present population is given to be 54000

$$\Rightarrow \frac{27x}{25} = 54000$$

$$\Rightarrow x = \frac{54000 \times 25}{27} = 2000 \times 25 = 50000$$

Therefore, population a year ago was 50000

Question 17: The value of a machine depreciates every year by 20%. If the present value of the machine be Rs 160000, what was its value last year?

Solution: Let value of machine last year be Rs x

It is given that value depreciates by 20% every year

$$\text{Thus, present value of machine} = 80\% \times x = \frac{80x}{100} = \frac{8x}{10} = \frac{4x}{5}$$

Also present value of machine is given to be Rs 160000

$$\Rightarrow \frac{4x}{5} = 160000$$

$$\Rightarrow x = \frac{160000 \times 5}{4} = 40000 \times 5 = 200000$$

Therefore, value of machine last year was Rs 200000

Question 18: An alloy contains 40% copper, 32% nickel and rest zinc. Find the mass of zinc in one kg of the alloy.

Solution: Mass of alloy = 1kg

Percentage of copper = 40%

Percentage of nickel = 32%

Percentage of zinc = $(100 - (40 + 32))\% = (100 - 72)\% = 28\%$

$$\text{Mass of zinc in 1 kg of alloy} = \frac{28}{100} \times 1 = 0.28 \text{ kg}$$

$$= 0.28 \times 1000 = 280g$$

Question 19: Balanced diet should contain 12% of proteins, 25% of fats and 63% of carbohydrates. If a child needs 2600 calories in his food daily, find in calories the amount of each of these in his daily food intake.

Solution: Total calories needed = 2600

Percentage of proteins = 12%

$$\text{Amount of proteins} = 12\% \times 2600 = \frac{12}{100} \times 2600 = 312 \text{ calories}$$

Percentage of fats = 25%

$$\text{Amount of fats} = 25\% \times 2600 = \frac{25}{100} \times 2600 = 650 \text{ calories}$$

Percentage of carbohydrates = 63%

$$\text{Amount of carbohydrates} = 63\% \times 2600 = \frac{63}{100} \times 2600 = 1638 \text{ calories}$$

Question 20: Gunpowder contains 75% nitre and 10% sulphur. Find the amount of gunpowder which carries 9 kg nitre. What amount of gunpowder would contain 2.5 kg sulphur?

Solution: Let the amount of gunpowder be x kg

So, x kg be the amount of gunpowder having 9 kg nitre

Percentage of nitre = 75%

$$\Rightarrow 75\% \times x = 9$$

$$\Rightarrow \frac{75x}{100} = 9$$

$$\Rightarrow x = \frac{900}{75} = 12 \text{ Kg}$$

Now, let x kg be the amount of gunpowder having 2.5 kg sulphur

Percentage of sulphur = 10%

$$\Rightarrow 10\% \times x = 2.5$$

$$\Rightarrow \frac{10x}{100} = 2.5$$

$$\Rightarrow x = \frac{2.5 \times 100}{10} = 25 \text{ Kg}$$

Question 21: Divide Rs 7000 among A, B and C such that A gets 50% of what B gets and B gets 50% of what C gets.

Solution: Let the amount C gets be Rs x

$$\text{Then, amount B gets} = 50\% \times x = \frac{50x}{100} = \frac{x}{2}$$

$$\text{And Amount A gets} = 50\% \times \frac{x}{2} = \frac{50}{100} \times \frac{x}{2} = \frac{x}{4}$$

$$\text{Given that } x + \frac{x}{2} + \frac{x}{4} = 7000$$

$$\Rightarrow \frac{4x+2x+x}{4} = 7000$$

$$\Rightarrow \frac{7x}{4} = 7000$$

$$\Rightarrow x = \frac{7000 \times 4}{7} = 4000$$

$$\text{Thus, A's share} = \frac{4000}{4} = 1000$$

$$\text{B's share} = \frac{4000}{2} = 2000$$

$$\text{C's share} = 4000$$

Question 22: Find the percentage of pure gold in 22-carat gold, if 24-carat gold is 100% pure.

Solution: Since 22- carat gold contains 22 parts out of 24 parts

$$\text{Therefore, percentage of pure gold in 22 carat gold} = \left(\frac{22}{24} \times 100\right)\% = \frac{275}{3}\% = 91\frac{2}{3}\%$$

Question 23: The salary of an officer is increased by 25%. By what per cent should the new salary be decreased to restore the original salary?

Solution: Let the original salary be Rs x

After increment of 25%,

Salary becomes $100 \left(1 + \frac{25}{100}\right)$

$$\Rightarrow 100 \left(\frac{100+25}{100}\right) = 125$$

Now, we have to restore the original salary, so let new salary be decreased by $x\%$

$$\Rightarrow 125 \left(1 - \frac{x}{100}\right) = 100$$

$$\Rightarrow \left(1 - \frac{x}{100}\right) = \frac{100}{125}$$

$$\Rightarrow 1 - \frac{100}{125} = \frac{x}{100}$$

$$\Rightarrow \frac{125-100}{125} = \frac{x}{100}$$

$$\Rightarrow \frac{25}{125} = \frac{x}{100}$$

$$\Rightarrow x = \frac{25 \times 100}{125} = 20\%$$

Exercise 9B

Question 1: $\frac{3}{5} = ?$

Solution: $\left(\frac{3}{5} \times 100\right)\% = 60\%$

Question 2: 0.8% when expressed as a decimal, is

Solution: $\frac{0.8}{100} = \frac{8}{1000} = 0.008$

Question 3: 6:5 when expressed as a percentage, is

Solution: Ratio = 6:5

$$\left(\frac{6}{5} \times 100\right)\% = 120\%$$

Question 4: 5% of a number is 9. The number is

Solution: Let a number be x

Then, according to given question,

$$5\% \times x = 9$$

$$\Rightarrow \frac{5x}{100} = 9$$

$$\Rightarrow x = \frac{900}{5} = 180$$

Question 5: What per cent of 90 is 120?

$$\text{Solution: } \left(\frac{120}{90} \times 100\right)\% = \frac{400}{3}\% = 133\frac{1}{3}\%$$

Question 6: What per cent of 10 kg is 250 g?

Solution: Since $1\text{kg} = 1000\text{g}$

$$\left(\frac{250}{10000} \times 100\right)\% = 2.5\%$$

Question 7: 40% of? = 240

$$\text{Solution: } 40\% \times x = 240$$

$$\Rightarrow \frac{40}{100} \times x = 240$$

$$\Rightarrow x = \frac{240 \times 100}{40} = 600$$

Question 8: ? % of 400 = 60

$$\text{Solution: } x\% \times 400 = 60$$

$$\Rightarrow \frac{x}{100} \times 400 = 60$$

$$\Rightarrow 4x = 60$$

$$\Rightarrow x = 15$$

Question 9: $(180\% \text{ of?}) \div 2 = 504$

Solution: $(180\% \times x) \div 2 = 504$

$$\Rightarrow \frac{(180\% \times x)}{2} = 504$$

$$\Rightarrow 180\% \times x = 504 \times 2$$

$$\Rightarrow \frac{180x}{100} = 1008$$

$$\Rightarrow x = \frac{1008 \times 100}{180} = 560$$

Question 10: 20% of Rs 800 =?

Solution: $20\% \times \text{Rs } 800 = \frac{20}{100} \times 800 = \text{Rs } 160$

Question 11: In an examination, Nitin gets 98 marks. This amounts to 56% of the maximum marks. What are the maximum marks?

Solution: Let the maximum marks be x

According to given question,

$$56\% \times x = 98$$

$$\Rightarrow \frac{56x}{100} = 98$$

$$\Rightarrow x = \frac{98 \times 100}{56} = \frac{9800}{56} = 175$$

Question 12: a number is first increased by 10% and then reduced by 10%. The number

(a) Does not change (b) decreases by 1% (c) increases by 1% (d) none of these

Solution: Let the number be x

When number is increased by 10%,

$$\text{New number} = 110\% \times x = \frac{110x}{100} = \frac{11x}{10}$$

Then, resulting number is decreased by 10%

$$\text{New number} = 90\% \times \frac{11x}{10} = \frac{90}{100} \times \frac{11x}{10} = \frac{99x}{100}$$

$$\text{Thus, net decrease} = x - \frac{99x}{100} = \frac{x}{100}$$

$$\text{Net decrease percentage} = \left(\frac{x}{100} \times \frac{1}{x} \times 100 \right) \% = 1\%$$

Question 13: A period of 4 hours 30 min is what per cent of a day?

$$\text{Solution: 4 hours 30 minutes} = 4 + \frac{30}{60} = 4 + \frac{1}{2} = \frac{9}{2} = 4.5 \text{ hours}$$

In a day there are 24 hours.

$$\text{Thus, } \left(\frac{4.5}{24} \times 100 \right) \% = \frac{225}{12} \% = \frac{75}{4} \% = 18\frac{3}{4} \%$$

Question 14: In an examination, 65% of the total examines passed. If the number of failures is 420, the total number of examinees is

Solution: Let the total number of examinees be x

Percentage of passed examinees = 65%

Thus percentage of failures = $(100-65) \% = 35\%$

Given that number of failures = 420

$$\Rightarrow 35\% \times x = 420$$

$$\Rightarrow \frac{35x}{100} = 420$$

$$\Rightarrow x = \frac{420 \times 100}{35} = 1200$$

Question 15: A number exceeds 20% of itself by 40. The number is

Solution: Let the number be x

Given that $x = (20\% \times x) + 40$

$$\Rightarrow x = \frac{20x}{100} + 40$$

$$\Rightarrow x - \frac{20x}{100} = 40$$

$$\Rightarrow \frac{80x}{100} = 40$$

$$\Rightarrow x = \frac{40 \times 100}{80} = 50$$

Question 16: A number decreased by $27\frac{1}{2}\%$ gives 87. The number is

Solution: Let the number be x

According to given question,

$$x - 27\frac{1}{2}\%x = 87$$

$$\Rightarrow x - \frac{55}{2}\%x = 87$$

$$\Rightarrow x - \frac{55x}{200} = 87$$

$$\Rightarrow x - \frac{11x}{40} = 87$$

$$\Rightarrow \frac{29x}{40} = 87$$

$$\Rightarrow x = \frac{87 \times 40}{29} = 120$$

Question 17: 0.05 is what per cent of 20?

Solution: $20 \times x\% = 0.05$

$$\Rightarrow \frac{x}{100} = \frac{0.05}{20}$$

$$\Rightarrow x = \frac{0.05 \times 100}{20} = 0.25\%$$

Question 18: One-third of 1206 is what per cent of 134?

Solution: $\frac{1}{3} \times 1206 = x\% \times 134$

$$\Rightarrow 402 = \frac{134x}{100}$$

$$\Rightarrow \frac{402 \times 100}{134} = x$$

$$\Rightarrow x = 300\%$$

Question 19: x% of y is y% of?

Solution: $x\% \times y = y\% \times x$

Question 20: What per cent of $\frac{2}{7}$ is $\frac{1}{35}$?

Solution: $x\% \times \frac{2}{7} = \frac{1}{35}$

$$\Rightarrow \frac{x}{100} \times \frac{2}{7} = \frac{1}{35}$$

$$\Rightarrow \frac{2x}{700} = \frac{1}{35}$$

$$\Rightarrow x = \frac{1}{35} \times \frac{700}{2} = 10\%$$

